

## [6.2] Use rectangular complex mode for faster results

Seemingly simple vector calculations can execute very slowly on the 89/92+ in Polar and Exact or Auto modes. This example

$$\frac{(250 \angle 85) * (121 \angle 3)}{(250 \angle 85) + (121 \angle 3)}$$

returns the correct result in less than 1 second in Approx, Degree and Polar modes. However, in Exact or Auto modes, the calculator might seem to 'hang up', but really the answer just takes a long time to calculate. A Texas Instruments TIcares representative offers this explanation.

*Thank you for your recent correspondence with Texas Instruments. Yes this behavior is possible: We internally calculate with expressions in the rectangular forms that are then converted to a polar form. Converting from a very complicated rectangular form to polar form in the exact or auto mode, can be extraneous on our TI-89 operating systems. Internal complex calculations are done in rectangular form. So, the polar complex numbers are converted to rectangular form. Then, the computation  $(a * b) / (a + b)$  is performed. Finally, the resulting rectangular complex number is converted to polar form. It's a difficult process. The result takes about 45 minutes on my TI-89 and looks like this.*

$$(30250 * \sqrt{62500 * (\cos(3))^2 * (\cos(5))^4 + (125000 * (\sin(5))^2 * (\cos(3))^2 + 60500 * \sin(5) * \cos(3) + 14641 * (\cos(5))^2 + 60500 * \sin(3) * \cos(5) + 62500 * (\sin(5))^4 * (\cos(3))^2 + 60500 * (\sin(5))^3 * \cos(3) + 14641 * (\sin(5))^2 + 62500 * (\sin(3))^2}) / (60500 * \sin(3) * \cos(5) + 60500 * \sin(5) * \cos(3) + 77141) < \operatorname{atan}((121 * \cos(5) + 250 * \sin(3)) / (250 * \cos(3) * (\cos(5))^2 + \sin(5) * (250 * \sin(5) * \cos(3) + 121))))$$

*One of the important lessons in computer algebra is that simple looking input may generate very large exact output and may take a great deal of time to compute. If fast times or small output is desired, it is sometimes best to interrupt a computation and approximate it. The approximate answer  $(103.416 < 27.1821)$  is generated in about 1 second.*