

### [6.39] Convert equations to a parameterized form

A function  $f(x,y) = 0$  can be 'parameterized' by converting it into two other functions  $x(t)$  and  $y(t)$ , where  $t$  is the parameter. These functions  $x(t)$  and  $y(t)$  are not necessarily unique; there may be many functions that give the same result  $f(x,y)$ . This function applies one possible parameterization of  $x$  and  $y$ , namely  $t = y/x$ .

```
parcurve(f,x,y)
Func
©ParCurve(f,x,y) parametrizes curve f(x,y)=0 as x(t),y(t)
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expr("solve("&string(f=y-t*x)&" and y-t*x=0,{&string(x)&",&string(y)&}))"
EndFunc
```

For example, to find a parametric expression for

$$x^3 + x^2 - y^2 = 0$$

use the call

```
parcurve(x^3+x^2-y^2,x,y)
```

which returns

$$x = t^2 - 1 \text{ and } y = (t^2 - 1) \cdot t \text{ or } x = 0 \text{ and } y = 0$$

The first two equations are the useful parameterizations; the second two are extraneous solutions.

*(Credit to Bhuvanesh Bhatt)*